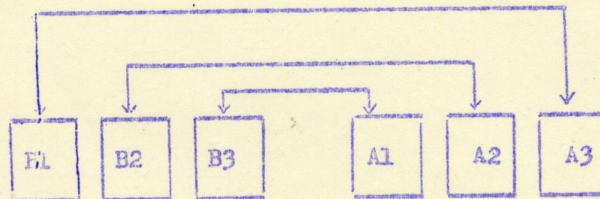


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CALCULATION OF THE PERIOD WITH DEVICE 39

1. Drive law :



- a. Number of divisions of the pin wheels A1,2,3
A1 = 23, A2 = 25, A3 = 27
- b. Number of divisions of the cipher wheels B1,2,3
B1 = 26, B2 = 26, B3 = 26
- c. Pin wheels A1,2,3 with their effective pins affect the course of cipher wheels B1,2,3.
- d. According to their divisions pins (t) on the pin wheels can be brought into an effective or ineffective position. That pin position is termed effective which checks the course of the cipher wheel.
- e. If all pins on pin wheel A1,2,3 are in the ineffective position then pin wheels A1,2,3 and cipher wheels B1,2,3 take one step each time a key is pressed.
- f. The number of effective pins is to be determined by the following formula: the number of divisions of the pin wheel less the number of effective pins must be prime to the number of divisions of the cipher wheel.
$$\text{Number of effective pins} = (tA - n) \neq tB.$$
- g. The total period is the product of the number of divisions of A1, A2, A3, B1, B2, B3. It breaks up into partial periods if the factors are not prime to one another. The sum of the partial periods is equal to the product of the divisions of all the wheels.

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In the present case 26^2 partial periods ($B2 \times B3$) of the length
 $A1 \times A2 \times A3 \times B1 = 23 \times 25 \times 27 \times 26 = 403676$ steps are derived.

The following example [in miniature] is intended to illustrate the computation.

Terms: A = pin wheels ($t1,2,3$)

B = cipher wheels ($t4,5,6$)

f = steps $B4,5,6$

t = number of divisions of $A1,2,3$ or $B1,2,3$

U = revolutions of A or B

n = number of effective pins on A

F = period

Ziffer = $A1,2,3, B4,5,6$

h = braking of the course of $B4,5,6$

$A1 = 5, A2 = 7, A3 = 9, B4 = 4, B5 = 4, B6 = 4.$

a. Periods without effective pins on the pin wheels:

$A1 = 5$ steps

$A2 = 7$ steps

$A3 = 9$ steps

$B4 = 4$ steps

$B5 = 4$ steps

$B6 = 4$ steps

b. Pin setting (effective pins)

$A1) At1 - n \neq Bt4 = 5 - 2 = 3 \neq 4$ (2 effective pins)

$A2) At2 - n \neq Bt5 = 7 - 4 = 3 \neq 4$ (4 effective pins)

$A3) At3 - n \neq Bt6 = 9 - 6 = 3 \neq 4$ (6 effective pins)

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c. Periods: $AlB_4 = t_1 \times t_4 = 5 \times 4 = 20$ steps.

A1 12345123451234512345
 o o o o o o o o effective pins
 B4 abbccdaabbccdaabccdd = 20 steps

A2 1234567123456712345671234567
 ooo o ooo o ooo o ooo o effective pins
 B5 aaaabbbccdddaabcccccddabbbcccd = 28 steps

A3 123456789123456789123456789123456789
 o o oo ooo o oo ooo o oo ooo o oo oo effective pins
 B6 aabbbcccccdddaabbbcccccdddaabbbcccccdddaa 36 steps

d. Period $Al,2,3 = t_1 \times t_2 \times t_3 = 5 \times 7 \times 9 = \underline{315 \text{ steps}}$

e. Revolutions of a pin wheel during the course of the period of $Al,2,3$ (315 steps).

$$\frac{F}{At_1} = \frac{UA_1}{5} = \frac{315}{5} = \underline{63UA_1}, \quad \frac{315}{7} = \underline{45UA_2}, \quad \frac{315}{9} = \underline{35UA_3}$$

Hence A_1 makes 63 revolutions, A_2 makes 45 and A_3 makes 35.

f. Number of effective pin functions (brakings of the cipher wheels $B_4,5,6$) within the course of one period of $Al,2,3$.

$$A_1: h_1 = U_1 \times n_{1A} = 63 \times 2 = \underline{126 \text{ steps}}$$

$$A_2: h_2 = U_2 \times n_{2A} = 45 \times 4 = \underline{180 \text{ steps}}$$

$$A_3: h_3 = U_3 \times n_{3A} = 35 \times 6 = \underline{210 \text{ steps}}$$

g. Number of steps of cipher wheels $B_4,5,6$.

$$B_1: f_1 = F - h_1 = 315 - 126 = \underline{189 \text{ steps}}$$

$$B_2: f_2 = F - h_2 = 315 - 180 = \underline{135 \text{ steps}}$$

$$B_3: f_3 = F - h_3 = 315 - 210 = \underline{105 \text{ steps}}$$

h. Number of revolutions of the cipher wheels within one period of $Al,2,3$.

$$B_4: B_4U = \frac{f_1}{Bt} = \frac{189}{4} = \underline{47 \frac{1}{4} \text{ revolutions}}$$

$$B_5: B_5U = \frac{f_2}{Bt} = \frac{135}{4} = \underline{33 \frac{3}{4} \text{ revolutions}}$$

$$B_6: B_6U = \frac{f_3}{Bt} = \frac{105}{4} = \underline{26 \frac{1}{4} \text{ revolutions}}$$

1. The period $Al,2,3, B_4,5,6$ is found from the product of the t 's.

Nevertheless the period of $Al,2,3, B_4,5,6$ has only run out when all drive wheels and cipher wheels have completed full revolutions at the same time. With 315 steps this is only satisfied for $Al,2,3$. Wheels $B_1,2,3$ have, as shown in paragraph h, made $1/4$, $3/4$, and $1/4$ too many revolutions. The period $Al,2,3$ must therefore be run through several times before all six wheels reach the initial position simultaneously.

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In running through the periods A1,2,3 the following steps are made.

Full Periods of A1,2,3	Steps	= Cipher Wheel Revolutions		
1	315	B4 47-1/4,	B5 33-3/4,	B6 26-1/4
2	630	B4 94-1/2,	B5 67-1/2,	B6 52-1/2
3	945	B4 141-3/4,	B5 101-1/4,	B6 78-3/4
4	1260	B4 188,	B5 135,	B6 105

The period A1,2,3 B4,5,6 yields, therefore:

$$P = A1 \times A2 \times A3 \times B4 \times B5 \times B6 = 5 \times 7 \times 9 \times 4 = \underline{1260 \text{ steps}}$$

k. In the preceding example each cipher wheel has 4 positions. With 3 cipher wheels there are therefore 4^3 effectively different positions, that means $4 \times 4 \times 4 = \underline{64 \text{ positions}}$. The pin wheels A1,2,3 have $5 \times 7 \times 9 = 315$ effectively different positions. The runs 1-4 shown in paragraph i had as a result that each of the 315 positions of the pin wheels A1,2,3 came into connection in each case with only 4 of the 64 possibilities of the cipher wheel.

E. g. The position of the pin wheels 1, 1, 1 only occurs in connection with the cipher wheel positions aaa, bcb, cbc, ddd.

4 of the 64 possibilities always occur together so that there are

$\frac{64}{4} = 16$ periods with a length of 1260 steps. This number 16 comes from the product $B5 \times B6 = 4 \times 4 = 16$. The breaking down of the period given by the product of all 6 wheels into 16 partial periods is the consequence of the equal number of divisions on B4,5,6.

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A1 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
B4 a b b c c d a a b b c d d a a b c c d d a b b c c d a a b b c d d a a
A2 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7
B5 a a a a b b c d d d d a a b c c c c d d a b b b b c c d a a a a b b c
A3 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 (23)
B6 a a b b c c c d d d d a a b b b c c c c d d a a a b b b b c c d d d a

1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
b c c d d a b b c c d a a b b c d d a a b c c d d a b b c c d a a b b
1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7
d d d d a a b c c c c d d a b b b b c c d a a a a b b c d d d d a a b
9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 (23)
a a a b b c c c d d d d a a b b b c c c c d d a a a b b b b c c d d d

1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
c d d a a b c c d d a b b c c d a a b b c d d a a b c c d d a b b c c
1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7
c c c c d d a b b b b c c d a a a a b b c d d d d a a b c c c c d d a
8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 (24)
a a a a b b c c c d d d d a a b b b c c c c d d a a a b b b b c c d d

1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
d a a b b c d d a a b c c d d a b b c c d a a b b c d d a a b c c d d
1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7 1 2 3 4 5 6 7
b b b b c c d a a a a b b c d d d d a a b c c c c d d a b b b b c c d
7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2 3 4 5 (23)
d a a a a b b c c c d d d d a a b b b c c c c d d a a a b b b b c c d

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1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5
 a b b c c d a a b b c c d d a a b c c d d a b b c c d a a b b c c d d a a
 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7
 a a a a b b c c d d d d a a b c c c c d d a b b b b c c d a a a a b b c
 6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5 6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 (23)
 d d a a a a b b c c c c d d d d a a b b b b c c c c d d a a a b b b b c c

1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5
 b c c d d a b b c c d a a b b c c d d a a b c c d d a b b c c d a a b b
 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7
 d d d d a a b c c c c d d a b b b b c c d a a a a b b c c d d d d a a b
 5|6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 3 (24)
 d d d a a a a b b c c c c d d d d a a b b b b c c c c d d a a a b b b b c

1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5
 c d d a a b c c d d a b b c c d a a b b c c d d a a b c c d d a b b c c
 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7
 c c c c d d a b b b b c c d a a a a b b c c d d d d a a b c c c c d d a
 4 5|6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 (23)
 c d d d a a a a b b c c c c d d d d a a b b b b c c c c d d a a a b b b b

1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5
 d a a b b c d d a a b c c d d a b b c c d a a b b c d d a a b c c d d
 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7
 b b b b c c d d a a a a b b c d d d d a a b c c c c d d a b b b b c c d
 3|4 5|6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1
 c c d d d a a a a b b c c c c d d d d a a b b b b c c c c d d a a a b b b

1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 1 2|3 4|5 **II III**
 a b b c c d a a b b c c d d a a b c c d d a b b c c d a a b b c d d a a **1 1 1 1**
 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 1|2|3|4 5|6 7 **1 1 1 1**
 a a a a b b c d d d d a a b c c c c d d a b b b b c c d a a a a b b c **c b d a**
 2 3|4 5|6|7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 2 3|4 5|6 7 8|9|1 **1 1 1 1**
 b c c d d d a a a a b b c c c c d d d d a a b b b b c c c c d d a a a b b **b e d a**

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A1 a

	a	b	c	d
a	///	///	///	///
b	///	///	/	///
c	///	///	///	///
d	///	///	/	///

A1 b

	a	b	c	d
A3 a	///	///	/	///
b	///	///	///	///
c	///	///	///	///
d	///	///	///	///

A1 c

	a	b	c	d
A2 a	///	///	///	///
b	///	///	///	///
A c	///	///	///	///
d	///	///	///	///

A1 d

	a	b	c	d
A3 a	///	///	///	///
A2 b	///	///	///	///
c	///	///	///	///
d	///	///	///	///

Run of 180 steps

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